

Kinetics study and modelling of sorghum grain hydration¹

Estudo e modelagem da cinética de hidratação de grãos de sorgo

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ABSTRACT - Sorghum grains were soaking to evaluate the effects of time and temperature on moisture and process modelling was made with different mathematical equations. Then, sorghum BRS 310 and BRS 655 were hydrated at 30 °C, 40 °C, 50 °C and 60 °C, for 12 hours. The hydration kinetics modelling with empirical equations of Peleg and Page and phenomenological equations of Diffusion and Omoto-Jorge were considered. The time and temperature affected significantly the hydration kinetics of grain sorghum. The Peleg and Diffusion models showed the best fitting for soaking and, therefore, these models were used to create generalized models. The effective diffusion coefficient of water during the grain sorghum hydration ranged from 2.02×10^{-11} to 6.34×10^{-11} $\text{m}^2 \cdot \text{s}^{-1}$ for BRS 310 and from 2.76×10^{-11} to 4.38×10^{-11} $\text{m}^2 \cdot \text{s}^{-1}$ for BRS 655 with activation energies of 11.52 and 31.21 $\text{kJ} \cdot \text{mol}^{-1}$, respectively.

Key words: *Sorghum bicolor*. Water diffusivity. Water absorption.

RESUMO - Neste estudo, grãos de sorgo foram hidratados para avaliar os efeitos do tempo e temperatura na umidade e modelar o processo com diferentes equações matemáticas. Para esse fim, as cultivares de sorgo BRS 310 e BRS 655 foram submetidas à hidratação nas temperaturas de 30 °C, 40 °C, 50 °C e 60 °C, por um período de 12 horas. O processo de hidratação foi modelado com as equações empíricas de Peleg e Page e com os modelos fenomenológicos de Difusão e Omoto-Jorge. O tempo e a temperatura afetaram significativamente a cinética de hidratação dos grãos de sorgo. Os modelos de Peleg e de Difusão apresentaram ajustes mais satisfatórios para o processo e, por isso, foram generalizados. O coeficiente de difusão efetivo de água nos grãos durante a hidratação variou de $2,02 \cdot 10^{-11}$ a $6,34 \cdot 10^{-11}$ $\text{m}^2 \cdot \text{s}^{-1}$ para a cultivar BRS 310 e de $2,76 \cdot 10^{-11}$ a $4,38 \cdot 10^{-11}$ $\text{m}^2 \cdot \text{s}^{-1}$ para a BRS 655 com energias de ativação de 31,21 e 11,52 $\text{kJ} \cdot \text{mol}^{-1}$, respectivamente.

Palavras-chave: *Sorghum bicolor*. Difusividade de água. Absorção de água.

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INTRODUCTION

Sorghum is the fifth most produced cereal in the world, behind only rice, corn, wheat and barley (FOOD AND AGRICULTURE ORGANIZATION OF THE UNITED NATIONS, 2015). This grain is often recommended as a safe food for celiac patients because it does not have the gluten proteins present in cereals of the genus *Triticum sp.* such as wheat, rye, and barley. Therefore, sorghum can be used in a variety of gluten-free foods such as beers, porridge, couscous, parboiled sorghum, starch and fermented and unfermented sorghum-based products, common in many countries in Africa, Asia and Central America (ARENDE; ZANNINI, 2013).

The pre-processing of sorghum for food manufacturing, such as starch, malt and flour, usually involves a stage of hydration of the grains. The moisture gain during hydration directly affects the quality of the final product (MIANO *et al.*, 2018).

Thus, research on the hydration behavior of sorghum grain is very important for the process control and optimization. Mathematical models have often been used for this purpose because they are able to predict water absorption as a function of time and temperature of hydration. Studies with different models are relevant to identify the one that describes the process more appropriately (BALBINOTI; JORGE, JORGE, 2018).

Empirical equations such as the Peleg model (BADAU; NKAMA; JIDEANI, 2005; KASHIRI; KASHANINEJAD; AGHAJANI, 2010; PATERO; AUGUSTO, 2015) and Page (KASHIRI; GARMAKHANY; DEGHANI, 2012), and theoretical Diffusion (FAN; CHU, SHELLENBERGER, 1963) were used in the hydration modelling of sorghum grains. However, the use of the Omoto-Jorge model and the comparative study employing several mathematical models, in order to find the best fit for the hydration of sorghum grains, have not yet been reported in the literature.

Thus, the objective of this work was to identify, among several mathematical models, the one that best describes the water absorption during hydration of sorghum grains, evaluating the effect of time and process temperature. To that end, two cultivars of sorghum of different classes were used: one of red sorghum grain, used in the manufacture of foodstuffs for human and animal consumption and a cultivar of brown grains of forage sorghum with characteristics directed to the production of animal silage, BRS 310 and BRS 655 respectively. Grains belonging to two distinct classes were used to identify if cultivars with very different characteristics had the same behavior during hydration kinetics and thusly, a single equation was promising to model a larger quantity of

sorghum cultivars. In addition, the water diffusivity in the grains and the activation energy of the hydration process were obtained.

MATERIALS AND METHODS

Samples

Hybrids BRS 310 (red grain sorghum) and BRS 655 (brown grain sorghum), two of the most produced sorghum cultivars in Brazil, were used in this study. The samples were cultivated in the Center-West of Brazil, crop 2014.

Hydration process

For the sorghum grain hydration experiment, approximately 500 g of sample of each cultivar were immersed in distilled water in a proportion of 1:3 (m/v) and hydrated for a period of 12 hours at temperatures of 30 °C, 40 °C, 50 °C and 60 °C. Samples were taken in triplicate and surface dried at 30-minute intervals over the first four hours and 60 minutes in the remainder of the experiment. The moisture (wet basis) was obtained by the oven-dry method at 105 °C for 24 hours in triplicate (ASSOCIATION OF OFFICIAL ANALYTICAL CHEMISTS, 2012).

Modelling

There are many models that may be appropriate to describe the hydration of cereals and vegetables. On choosing the model best fit model, small deviations from experimental data and the model simplicity of the model must be taken into account. Empirical models have been extensively used for their simplicity, while theoretical or phenomenological models bring greater physical significance to the equation (KASHIRI; KASHANINEJAD; AGHAJANI, 2010).

Empirical models

Peleg's model

The non-exponential empirical model most commonly used to describe the hydration of vegetables and grains was developed by Peleg (1988) to predict the soaking of powdered milk and rice grains (Equation 1).

$$M_t = M_0 + \frac{t}{k_1 + K_2} \quad (1)$$

Where: t is the time (h); M_t , the moisture at time t (% w.b.); M_0 , initial moisture (% w.b.); k_1 , the constant rate of Peleg (h.% w.b.⁻¹) and k_2 , the Peleg capacity constant (% w.b.⁻¹).

Page's Model

In 1949, Glen E. Page developed an equation to describe the drying of corn grains (Equation 2), which is currently one of the most used to describe the hydration of foods (CUNEO; OLIVEIRA; OLIVEIRA, 1998).

$$\frac{M_t - M_e}{M_0 - M_e} = e^{(-k_p t^N)} \quad (2)$$

Where: M_t is the moisture at time t (% w.b.); M_e is the equilibrium moisture (% w.b.); M_0 the initial moisture (% w.b.); t is the time (h); k_p (h^{-1}) is the absorption rate of the process and N is a dimensionless constant.

Phenomenological Models

Omoto-Jorge's model

A phenomenological model was developed by Omoto, Andrade and Jorge (2009) to describe the hydration of peas from a mass balance in the grain in a transient regime based on the mass transfer by convection. Considering a mass flow $N_A = K_s (\rho_{eq} - \rho_A)$, where ρ_A is the mass water concentration in the grain ($\text{g}\cdot\text{cm}^{-3}$), ρ_{eq} is the mass water concentration in the equilibrium ($\text{g}\cdot\text{cm}^{-3}$) and K_s is the mass transfer coefficient ($\text{cm}\cdot\text{min}^{-1}$), considering the spherical grain of radius r , and the initial condition $\rho_A = \rho_{A0}$ at $t = 0$:

$$\frac{d(p_A)}{dt} = \frac{3k_s}{r} (p_{Aeq} - p_A) \quad (3)$$

Diffusion Model, Effective Diffusion Coefficient and Activation Energy

Considering Fick's diffusion laws and mass balance on the grain surface, the diffusion in a spherical body, whereas the transport of water only in the radial direction, can be represented by Equation 4 (CRANK, 1975).

$$\frac{\partial M}{\partial t} = D \left(\frac{\partial^2 M}{\partial a^2} + \frac{2}{a} \frac{\partial M}{\partial a} \right) \quad (4)$$

Where: M is the humidity; a is the radial coordinate (m) and t the time (h).

Assuming the sorghum grain have spherical geometry, particle volume is constant, effective diffusion coefficient (D_{ef}) independent of concentration, grain surface comes to equilibrium instantaneously right after its immersion and following initial and boundary conditions:

- Initial condition: grain moisture is uniform, M_0 ;
- Boundary condition: the grain surface maintains equilibrium moisture, M_e .

The analytical solution for Equation 4 is Equation 5.

$$\frac{M_t - M_e}{M_0 - M_e} = \frac{6}{\pi^2} \sum_{n=1}^{\infty} \exp\left(-\frac{D_{ef} n^2 \pi^2 t}{r^2}\right) \quad (5)$$

Where: r is the radius of the grain (m).

The dependence between grain diffusivity and hydration temperature can be described by Arrhenius equation (Equation 6).

$$D_{ef} = D_0 e^{\left(-\frac{E_a}{RT}\right)} \quad (6)$$

Where: D_{ef} is the effective diffusivity ($\text{m}^2\cdot\text{s}^{-1}$), D_0 is the proportionality constant ($\text{m}^2\cdot\text{s}^{-1}$), E_a is the activation energy ($\text{kJ}\cdot\text{mol}^{-1}$), T is the temperature (K) and R is the gas constant.

Validation and model choice

The validation of the models was performed by Analysis of Variance (ANOVA) and residue analysis. The adjustment level was evaluated by the coefficient of determination (R^2) and by the deviation analysis performed by means root mean square error (RMSE) (7) and the relative mean error (P) (8).

$$RMSE = 100 \sqrt{\frac{1}{n} \sum \left(\frac{M_{\text{exp}} - M_{\text{pre}}}{M_{\text{exp}}} \right)^2} \quad (7)$$

$$P = \frac{100}{n} \sum \left(\frac{M_{\text{exp}} - M_{\text{pre}}}{M_{\text{exp}}} \right) \quad (8)$$

Where: M_{exp} is the moisture measured experimentally, M_{pre} is the moisture predicted by the model, n is the number of experimental points and GRL is the degree of freedom.

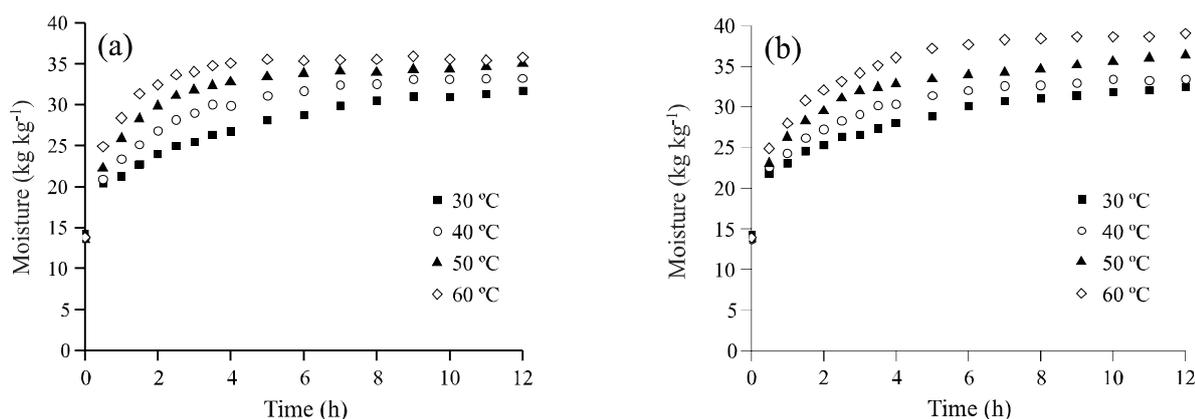
Statistical Analyses

The effect of time and temperature on water uptake by the grains was determined using the analysis of variance (ANOVA) at 95% significance level, with analysis of differences between the means by the Tukey test, also at 95% significance level.

RESULTS AND DISCUSSION

Hydration kinetics

The moisture content in sorghum BRS 310 (Figure 1a) and BRS 655 (Figure 1b) during hydration at different temperatures show a initial high rate of water absorption ($\text{g}\cdot\text{h}^{-1}$) that decreases with the approximation of equilibrium moisture (Figure 1).

Figure 1 - Moisture of sorghum cultivars BRS 310 (a) and BRS 655 (b) at different temperatures during the hydration process

Several mass transport mechanisms are responsible for the migration of water into the grain during the soaking, such as capillarity, liquid diffusion and vapor diffusion. However, the hydration process has been considered a phenomenon mainly controlled by liquid diffusion (OLI *et al.*, 2004; PRASAD; VAIRAGAR; BERA, 2010; RESENDE; CORRÊA, 2007).

On the other hand, the high initial absorption rate probably occurs due to the effect of capillarity that accelerates water penetration into the grain (FAN; CHU; SHELLENBERGER, 1963; KASHIRI; GARMAKHANY; DEGHANI, 2012; PRASAD; VAIRAGAR; BERA, 2010). First, the grain channels and cracks allow a rapid inflow of water, increasing the initial absorption rate. Thus, until the complete saturation of the porous structure, the water absorption is extremely accelerated (BECKER, 1960; KASHANINEJAD; DEGHANI; KASHIRI, 2009). In addition, the diffusion of water inside the grain is also fast because the initial driving force of the process is higher (KASHIRI; GARMAKHANY; DEGHANI, 2012; PRASAD; VAIRAGAR; BERA, 2010).

After the first hour of hydration, there was a reduction in the amount of water absorbed, which is probably due to the saturation of the grain pores, which reduces the effect of capillarity, and to the increase of water concentration inside the grain, which decreases the gradient of concentration in the grain (KASHANINEJAD; DEGHANI; KASHIRI, 2009; KASHIRI; GARMAKHANY; DEGHANI, 2012; PRASAD; VAIRAGAR; BERA, 2010).

Thus, the immersion time of the sorghum grains interfered significantly in the moisture gain for both

cultivars ($p < 0.05$). Sorghum also absorbed more water at higher temperatures during hydration ($p < 0.05$). These observations are in agreement with other researches (MONTANUCI; JORGE; JORGE, 2013; RESENDE; CORRÊA, 2007). This fact occurs because the temperature increase expands and softens the grain, increasing the water absorbed (KASHANINEJAD; DEGHANI; KASHIRI, 2009).

Then, the hydration temperature affects the moisture of the sorghum grains BRS 310 and BRS 655 and can be used to reduce the process time required for the grain to absorb the desired amount of water.

Hydration kinetics modeling

The four equations selected for the sorghum hydration process (Peleg, Page, Diffusion and Omoto-Jorge) presented values of calculated F value greater than F statistic from the Analysis of Variance at 95% and 99% significance level. These proving that the regression is significant and the residuals are small. In addition, the residuals were randomly dispersed as a function of time, validating the models studied in this work. The values of coefficient of determination (R^2), root mean square error (RMSE) and relative mean error (P) can be observed in Table 1.

The models presented R^2 between 81.5% and 99.9% and the Peleg model obtained the highest values among the models used. In order for a model to be considered acceptable to describe the process, the value of the relative mean error (P) should be less than 10% and the root of the mean error value (RMSE) less than 5% (MAIORANO; MANCINI; REYNERI, 2010). Moreover, when P is less than 5%, a better fit is assigned to the model (LOMAURO; BAKSHI; LABUZA, 1985).

Table 1 - Parameters of the models as a function of the hydration temperature of sorghum grains

Model	Cultivar	Temperature (°C)	P* (%)	RMSE** (%)	R ² (%)
Peleg	BRS 310	30	1.87	3.16	99.2
		40	0.93	1.33	99.9
		50	0.61	0.72	99.9
		60	1.88	2.88	99.9
	BRS 655	30	2.30	3.64	99.4
		40	1.34	2.35	99.9
		50	1.37	1.83	99.8
		60	1.01	1.57	99.9
Page	BRS 310	30	2.05	2.64	95.4
		40	1.24	1.78	96.8
		50	0.77	0.98	98.8
		60	0.52	0.75	97.4
	BRS 655	30	1.75	2.36	95.5
		40	1.11	1.68	97.9
		50	0.64	0.81	98.5
		60	0.82	1.25	99.0
Diffusion	BRS 310	30	2.15	2.81	98.4
		40	1.57	2.71	99.2
		50	1.59	2.98	99.1
		60	1.32	2.84	99.3
	BRS 655	30	1.72	2.85	98.6
		40	1.21	2.69	99.3
		50	2.00	3.22	98.7
		60	1.21	3.14	99.5
Omoto-Jorge	BRS 310	30	4.08	6.45	98.2
		40	2.63	4.56	96.5
		50	6.68	9.75	81.5
		60	2.29	4.38	90.7
	BRS 655	30	5.93	9.04	96.6
		40	4.70	7.92	96.4
		50	7.15	10.69	87.0
		60	6.29	9.75	93.3

* Relative average error; ** Square root of mean square error

Thus, the Peleg, Page and Diffusion models were able to predict the hydration process with good adjustments because they presented values of P and RMSE of less than 5% (MAIORANO; MANCINI; REYNERI, 2010).

In order to choose the most appropriate model, the one with the highest coefficient of determination (R²) and the lowest values of P and RMSE (KASHANINEJAD

et al., 2007; PRASAD; VAIRAGAR; BERA, 2010) are taken into account. The Peleg model showed the highest R² values for both cultivars, while the Page, Peleg and Diffusion models showed lower SE, RMSE or P at certain temperatures.

Thus, to compare a phenomenological and an empirical model, the empirical model of Peleg and the phenomenological model of Diffusion were used

to develop a generalized equation of the process for obtaining the best adjustments.

Generalized models

A generalized model provides information on grain moisture during the hydration step as a function of time and temperature, and is of interest to the industry of starch, malt and sorghum flour.

In order to obtain the generalized models of Peleg and Diffusion, the parameters of each model proportional to the rate of absorption of water in the grain (k_1 for Peleg and D_{ef} for the model of Diffusion) could be related to the temperature with Arrhenius equation, by means of Equations 9 and 10 for the Peleg model, and 11 and 12 for the diffusion model, with good fit (Table 2).

The equations obtained R^2 values greater than 80% and relative mean error (P) less than 6% for the two sorghum cultivars (Table 2).

To obtain the generalized Peleg model, the parameter k_2 could be related to temperature by a linear equation (RESENDE; CORRÊA, 2007). The R^2 values were greater than 95% and P values were lower than 7% (Table 3).

The generalized Peleg and Diffusion models are presented in Figures 2 and 3 for cultivars BRS 310 and BRS 655, respectively.

Both generalized models were also validated because they presented random residuals and calculated F values larger than the F statistic values, according to

Table 2 - Parameters of Peleg and Diffusion generalized models

Cultivar	Model	Parameter	Equation	R^2 (%)	*P (%)
BRS 310	Peleg	k_1	$1/k_1 = 3.10^9 \cdot e^{(-5892/T)}$ (9)	99.3	4.39
	Difusão	D_{ef}	$D_{eff} = 2,90 \cdot e^{(-3754/T)}$ (10)	99.2	2.87
BRS 655	Peleg	k_1	$1/K_1 = 1.10^5 \cdot e^{(-2758/T)}$ (11)	96.1	5.10
	Difusão	D_{ef}	$D_{eff} = 1,77 \cdot e^{(-1393/T)}$ (12)	80.0	4.58

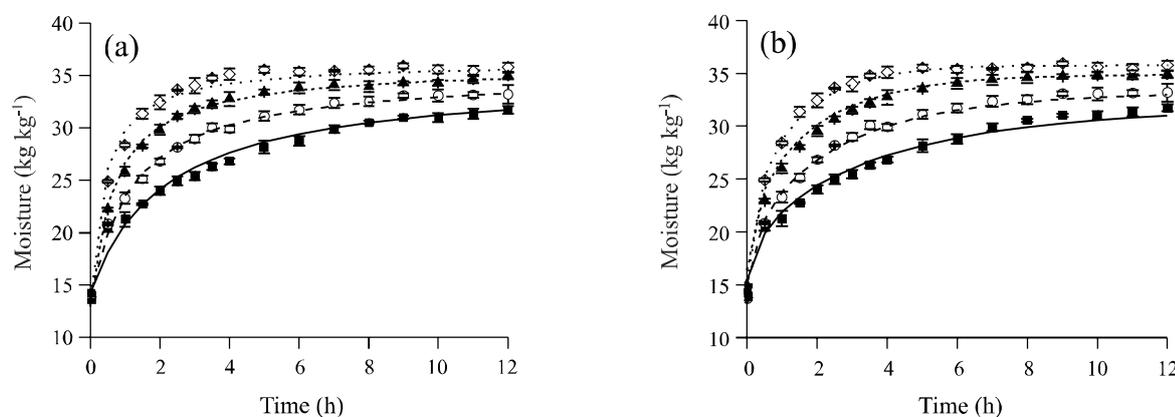
* Average relative error

Table 3 - k_2 parameter of the Peleg generalized equation for the hydration of sorghum grains

Cultivar	Parameter	Equation	R^2 (%)	P (%)
BRS 310	k_2	$k_2 = -2 \times 10^{-4}T + 5.45 \times 10^{-2}$ (13)	95.2	6.07
BRS 655	k_2	$k_2 = -4 \times 10^{-4}T + 6.17 \times 10^{-2}$ (14)	99.1	0.47

* Average relative error

Figure 2 - Generalized model of Peleg (a) and Diffusion (b) for the moisture as a function of the hydration time of the sorghum grains of cultivar BRS 310 at different temperatures



ANOVA at the 95% and 99% significance level. The Peleg and Diffusion models were generalized successfully, with their parameters presenting mean relative error and root mean square error values lower than 3%. The Peleg model presented P values of 1.29% and 1.53% for cultivars BRS 310 and BRS 655, respectively, whereas for the Crank model, the P value was 1.70% for cultivar BRS 310 and 1.81% for cultivar BRS 655. Similarly, the Peleg model presented deviations from the root mean square error (2.14% for BRS 310 and 2.53% for BRS 655) slightly lower than the Diffusion model (2.8% for BRS 310 and 3.12% for BRS 655), but with very similar and excellent fits for both.

Figure 4 reinforces the similarity between the deviations of the generalized Peleg and Diffusion models that fall within the range of 5% for BRS 310 and BRS 655 cultivars. Therefore, the models can be used to predict moisture as a function of the time and hydration temperature of sorghum cultivars BRS 310 and BRS 655 under the conditions studied because they presented excellent fits. The generalized model of Peleg showed slightly smaller deviations in relation to the generalized model of Diffusion and, therefore, it was the best one to describe the process of hydration of sorghum studied, besides being easy to use in the industry for its simplicity. On the other hand, the diffusion model

Figure 3 - Generalized model of Peleg (a) and Diffusion (b) for moisture as a function of time during the hydration of sorghum grains of cultivar BRS 655 at different temperatures

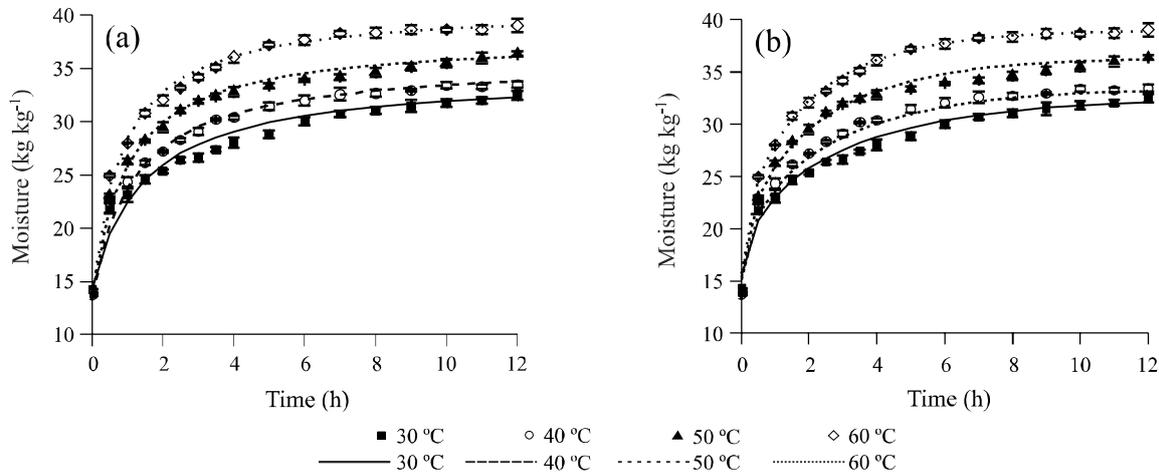
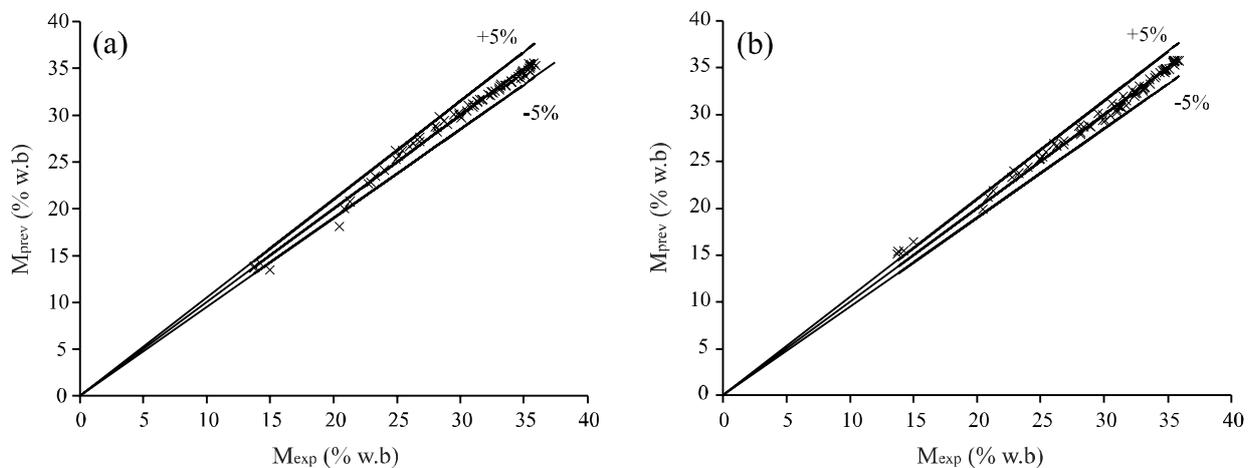


Figure 4 - Comparison between experimental (M_{exp}) and predicted (M_{prev}) moisture values for the Peleg (a) and Diffusion (b) generalized models of BRS 310 with 5% deviation



presented higher but very similar deviations and, because it is phenomenological, it has greater physical meaning. This model provide the effective diffusion coefficient, an important parameter for optimization of industrial processes and equipment projects, showing to be the most suitable to the hydration of grains in the cultivars presented.

Effective Diffusion Coefficient (D_{ef}) and Activation Energy

D_{ef} is an important property used to optimize the processes involving water transport inside the grains. D_{ef} value is named apparent because it comprises all the factors involved in the process, besides being the representation of the water diffusivity by a simple average property (YILDIRIM; ÖNER; BAYRAM, 2011).

The effective diffusion coefficient of the BRS 310 sorghum grain increased during hydration with increasing temperature (Table 4), as observed in soybean (GOWEN *et al.*, 2007), rice (KASHANINEJAD *et al.*, 2007) and chickpeas (PRASAD; VAIRAGAR; BERA, 2010). However, for the cultivar BRS 655 its value decreased from 40 °C to 50 °C, a temperature drop also reported by Thakur and Gupta (2006) in brown rice grains and Montanuci, Jorge and Jorge (2015) in barley.

The diffusion coefficients ranged from 2.017×10^{-11} to $6.342 \times 10^{-11} \text{ m}^2 \text{ s}^{-1}$ for cultivar BRS 310 and from 2.755×10^{-11} to $4.387 \times 10^{-11} \text{ m}^2 \text{ s}^{-1}$ for cultivar BRS 655. Becker (1960) observed values of $3.63 \times 10^{-11} \text{ m}^2 \text{ s}^{-1}$ in wheat grains, Montanuci, Jorge and Jorge (2015) and Mayolle *et al.* (2012) values between 5.14×10^{-12} and $10.80 \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$ in barley grains and Kashiri, Kashaninejad and Aghajani (2010)

Table 4 - Effective diffusion coefficient of the Diffusion model as a function of the hydration temperature of the sorghum grains

Cultivar	Temperature (°C)	*Def ($10^{-11} \text{ m}^2 \text{ s}^{-1}$)
BRS 310	30	2.017 ± 0.008
	40	3.098 ± 0.010
	50	4.113 ± 0.015
	60	6.342 ± 0.025
BRS 655	30	2.755 ± 0.012
	40	3.907 ± 0.012
	50	3.802 ± 0.015
	60	4.387 ± 0.120

* Effective diffusion coefficient

values from 2.22×10^{-12} to $8.32 \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$ in sorghum grains. Close values show that cereals have similar effective diffusion coefficients (KASHANINEJAD *et al.*, 2007).

The activation energy (E_a) of the grain hydration was obtained from the relation between the D_{ef} and the temperature by Arrhenius equation (Equation 6) (KASHANINEJAD *et al.*, 2007; KHAZAEI; MOHAMMADI, 2009; PRASAD; VAIRAGAR, (2006). The fit for this relationship was adequate, with a determination coefficient higher than 80% for both cultivars and P values lower than 5% (Table 2).

Typical E_a values observed in some researchs are presented in Table 5 along with the results obtained in this work. The estimated values of E_a for sorghum grains studied were $31.21 \text{ kJ} \cdot \text{mol}^{-1}$ for cultivar BRS 310

Table 5 - Activation energy of the hydration process of some cereals in different temperature ranges

Cereal	Variety	Temperature (°C)	*Ea ($\text{kJ} \cdot \text{mol}^{-1}$)	Author
Sorghum	ICSV 111	10-50	3.88	Badau, Nkama e Jideani (2005)
Sorghum	-	10-50	24.21	Kashiri, Kashaninejad e Aghajani (2010)
Sorghum	White Kafir	0-100	8.34	Fan, Chu e Shellenberger (1963)
	Atlas		8.42	
Wheat	-	-	11.98	Maskan (2002)
Corn	DKB 245PRO	40-67	31.95	Marques, Jorge e Jorge (2014)
	DKB 390PRO		31.96	
	DKB 240PRO		34.07	
Barley	BRS ELIS	10-35	51.67	Montanuci, Jorge e Jorge (2015)
Sorghum	BRS 310	30-60	31.21	This work
	BRS 655		11.52	

* Activation Energy

and $11.52 \text{ kJ}\cdot\text{mol}^{-1}$ for cultivar BRS 655, which obtained lower E_a , indicating its lower sensitivity to the temperature change in the hydration process carried out between $30 \text{ }^\circ\text{C}$ and $60 \text{ }^\circ\text{C}$.

Compared with other cereals (Table 5), the estimated E_a of sorghum grains of cultivar BRS 655 presented a similar value in relation to wheat grains (MASKAN, 2002), while cultivar BRS 310 obtained E_a value close to observed by Marques, Jorge and Jorge (2014) in corn grains. Both cultivars showed lower E_a values than those observed in grains of barley by Montanuci, Jorge and Jorge (2015).

Sorghum grain showed activation energies close to that of cultivar BRS 655 (FAN; CHU; SHELLENBERGER, 1963). Badau, Nkama and Jideani (2005) observed a lower value of E_a ($3.88 \text{ kJ}\cdot\text{mol}^{-1}$), while Kashiri, Kashaninejad and Aghajani (2010) found an E_a of $24.21 \text{ kJ}\cdot\text{mol}^{-1}$ in hydration at temperatures ranging from $10 \text{ }^\circ\text{C}$ to $50 \text{ }^\circ\text{C}$ in sorghum grain too.

It is clear that the differences between the activation energies of the hydration process are more expressive among the cultivars within the same species than among the different cereals. Differences in E_a values may occur due to variations in the chemical composition and grain structure between the cultivars (MONTANUCI; JORGE; JORGE, 2013).

CONCLUSIONS

1. Hydration time and temperature affect the moisture of the sorghum grains studied and a higher temperature decreased the time required to reach the desired moisture between $30 \text{ }^\circ\text{C}$ and $60 \text{ }^\circ\text{C}$;
2. Empirical equations of Peleg and Phenomenological equations of Diffusion and Omoto-Jorge were validated to model the process, under the conditions and cultivars studied, by the F test, randomness of the residues and high R^2 value. The Omoto-Jorge model had never been fitted before for the hydration of sorghum grains;
3. Peleg and Diffusion model obtained the best fits in the moisture prediction of the sorghum grains during the hydration. In addition, they were generalized, with similar deviations to predict water absorption as a function of process time and temperature, each model with its advantages: Peleg model is simpler while Diffusion model has physical meaning and it is able to provide the diffusion coefficient of the process;
4. The effective diffusion coefficient increased from $2.02 \text{ m}^2 \text{ s}^{-1}$ to $6.34 \text{ m}^2 \text{ s}^{-1}$ in BRS 310 sorghum and from 2.76 to $4.39 \text{ m}^2 \text{ s}^{-1}$ in BRS 655 sorghum with

the increase of hydration temperature from $30 \text{ }^\circ\text{C}$ to $60 \text{ }^\circ\text{C}$;

5. The effective diffusion coefficients could be related to the temperature by Arrhenius equation. The activation energy (E_a) of the hydration process was $11.52 \text{ kJ}\cdot\text{mol}^{-1}$ for cultivar BRS 655 and $31.21 \text{ kJ}\cdot\text{mol}^{-1}$ for cultivar BRS 310;
6. In this work, it was verified that two sorghum cultivars with distinct characteristics and classifications were well represented during hydration by the Diffusion and Peleg models. This result shows that these two models are promising for the industrial process of hydration of other sorghum cultivars.

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